# Interaction-Free Ion-Photon Gates (Milan, May 17, 2007) 

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## Early Interaction-Free Experiments

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## Ring Resonator

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Reflected portion of the incoming beam:

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"All" round trips: interference (a geometric progression) - the total amplitude $\left(D_{r}\right)$ :

$$
B=\sum_{i=0}^{\infty} B_{i}=-A \sqrt{R} \frac{1-e^{i \psi}}{1-R e^{i \psi}}
$$

## Resonator Int.-Free Experiments

$\psi=\left(\omega-\omega_{\text {res }}\right) T$ - phase per round-trip (r-t); $\omega$
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(b)

ABS


## Classical Efficiency



The efficiency of the suppression of the reflection into $D_{r}$ when there is no object in the resonator; $\rho$ is the measure of losses

## Let object be atom

${ }^{87} \mathrm{Rb}$ has closed shells up to $4 p$ and an electron in ground state $5 s(\mathbf{J}=\mathbf{L}+\mathbf{S})$; We consider only one excited state: $5 p_{1 / 2}$.

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External magnetic field B splits the levels into magnetic Zeeman sublevels:
$m=-F,-F+1, \ldots, F$.

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When a photon is emitted, the same selection rules must be observed.

## Atom vs. photon (ctnd.)

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we arrive at the Hamiltonian

$$
\hat{H}=\frac{\hbar}{2}\left[\begin{array}{ccc}
0 & \Omega_{1}(t) & 0 \\
\Omega_{1}(t) & 2 \Delta & \Omega_{2}(t) \\
0 & \Omega_{2}(t) & 0
\end{array}\right]
$$

$\Omega_{1}$ and $\Omega_{2}$ are Rabi frequencies

## Excited state drops out

One of the eigenstates of the Hamiltonian is

$$
\left|\Psi^{0}\right\rangle=\frac{1}{\sqrt{\Omega_{1}^{2}(t)+\Omega_{2}^{2}(t)}}\left(\Omega_{2}(t)\left|g_{1}\right\rangle-\Omega_{1}(t)\left|g_{2}\right\rangle\right)
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It depends only on "dark states" $\left|g_{1}\right\rangle$ and $\left|g_{2}\right\rangle$
We can use this to obtain a direct transfer of electrons from $\left|g_{1}\right\rangle$ to $\left|g_{2}\right\rangle$ without either emitting or absorbing photons on the part of atom in the following way-Stimulated Raman adiabatic passage (STIRAP).

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This can be described by

$$
\begin{array}{ll}
\left|\left\langle g_{1} \mid \Psi^{0}\right\rangle\right|^{2}=1 & \text { for } \quad t \rightarrow-\infty \\
\left|\left\langle g_{2} \mid \Psi^{0}\right\rangle\right|^{2}=1 & \text { for } \quad t \rightarrow+\infty
\end{array}
$$

Adiabatic complete population transfer $\left|g_{1}\right\rangle \rightarrow\left|g_{2}\right\rangle$ is STIRAP:

## STIRAP $\left|g_{1}\right\rangle \leftrightarrow\left|g_{2}\right\rangle$



## Interaction-free "excitation"

A left-hand circularly polarized photon could excite an atom from its ground state $\left|g_{1}\right\rangle$ to its excited state $|e\rangle$ and a right-hand circularly polarized photon could excite the atom from $\left|g_{2}\right\rangle$ to $|e\rangle$.

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So an $L$-photon will "see" the atom in $\left|g_{1}\right\rangle$ but will not "see" it when it is in $\left|g_{2}\right\rangle$. With an $R$-photon, the opposite is true.

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We can induce a change of the atom from $\left|g_{1}\right\rangle$ to $\left|g_{2}\right\rangle$ and back by a STIRAP process, with two additional external laser beams

## State notation

We feed our resonator with $+45^{\circ}$ and $-45^{\circ}$ linearly polarized photons.

In front of an atom we place a quarter-wave plate (QWP) to turn a $45^{\circ}$-photon into an $R$-photon and a $-45^{\circ}$-photon into an $L$-photon.

Behind the atom we place a half-wave plate (HWP) to change the direction of the circular polarization and then another QWP to transform the polarization back into the original linear polarization.

## State notation (ctnd.)

We denote the atom states as follows:

$$
|0\rangle=\left|g_{1}\right\rangle, \quad|1\rangle=\left|g_{2}\right\rangle
$$

They are control states; atom is control qubit.
We denote the photon states as follows:

$$
|0\rangle=\left|45^{\circ}\right\rangle, \quad|1\rangle=\left|-45^{\circ}\right\rangle
$$

They are target states; photons are target qubits.
For example, $|01\rangle$ means that the atom is in state $\left|g_{1}\right\rangle$ and the photon is polarized along $-45^{\circ}$.

## Interaction-free CNOT gate


(a) The atom is in state $\left|g_{1}\right\rangle$ and can absorb $|1\rangle$; (b) The atom is in state $\left|g_{2}\right\rangle$ and can absorb $|0\rangle$;

$$
|00\rangle \rightarrow|00\rangle,|01\rangle \rightarrow|01\rangle,|10\rangle \rightarrow|11\rangle,|11\rangle \rightarrow|10\rangle
$$

