Comparative study of organic metals and high-$T_c$ cuprates

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A B S T R A C T

The Bechgaard salts and the high $T_c$ cuprates are described by two and three band models, respectively, with the lowest band (nearly) half filled. In organics the interactions are small, while in cuprates the repulsion $U_d$ on the Cu-site is the largest energy. The Mott-AF state is stable in undoped materials in both cases. In the metallic phase of cuprates the $U_d \to \infty$ limit produces a moderate effective repulsion. The theories of the coherent SDW and charge-transfer correlations in the metallic phases of organics and cuprates are thus similar. In (undoped) organics those correlations are associated with commensurate 2$k_F$ SDW and 4$k_F$ bond or site modes. The corresponding modes in metallic cuprates are the incommensurate SDW and in particular $O_x/O_y$ quadrupolar charge transfer with wave vector $2q_{gyw} = q_0 + G$. They are enhanced for dopings $x > 0$, which bring the Fermi level close to the van Hove singularity. Strong coupling to the lattice associates the static incommensurate $O_x/O_y$ charge transfer with collinear “nematic” stripes. In contrast to organics, the coherent correlations in cuprates compete with local $d_{10} \leftrightarrow d_9$ quantum charge-transfer disorder.

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1. Introduction

The high-$T_c$ cuprates are usually described by the Emery model [1] where the role similar to the external dimerization [2] in the Bechgaard salts is played by the Cu–O hopping $t_{pd}$, which puts two oxygens in the CuO$_2$ unit cell and makes the lowest of three bands half filled. The weak coupling theory at zero doping $x$ is then a quite straightforward analogue [3–6] of the 1D theory, provided that their spins are opposite. This leads to the fact that two holes on the neighboring Cu-site are on the O-sites, i.e., that 

$$
U_d = \infty
$$

and can be interpreted as a retardation (kinematic) effect.

2. $U_d = \infty$ slave particle theory of the metallic phase

We have carried out the corresponding systematic theory which starts from the $n_{pd}^{(0)} = 0$ unperturbed metallic ground state by using the slave particles. This time dependent diagrammatic approach, of infinite order in the perturbation $t_{pd}$, requires the use of the spinless fermion-Schwinger boson representation in order to avoid the degeneracy of the $n_{pd}^{(0)} = 0$ unperturbed ground state in the overcomplete slave particle Hilbert space. The advantage of this representation is that the perturbation theory is manifestly translationally invariant at each stage, and ultimately locally gauge invariant. The disadvantage is that the three sorts of particles involved, $p^\pm$-fermions, $s$-spinless fermions and Schwin-
ger's $b^\pm$-bosons are distinguishable, i.e., that the Cu–O anticommutation rules are replaced by commutations. The theory has to be therefore antisymmetrized a posteriori. Here, we only quote the results.

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First, the omission of the Cu–O anticommutation rules is irrelevant in the lowest $r = 1$ order of the Dyson perturbation theory. The reason is that the Cu site is initially empty, while one particle on Cu is required for anticommutation and two for $U_g$ interaction. This makes the $r = 1$ expression for physical single-particle propagators strictly equivalent to the result of the $tpd$ hybridized HF theory. The HF theory is expressed in terms of two hybridized propagators, one which starts and finishes with the appropriately weighted propagation on the $o$-sites ($tpd$ propagator hereafter) and the other begins and ends on the Cu-sites ($dpd$ propagator). Both propagators are characterized by the three $i = L, I, U$ bands of poles (branches) at $\omega_n^{(i)}$ [8]. This holds irrespectively of the average HF occupation $n_d^{(i)}$ of the Cu-site associated with the chemical potential $\mu^{(i)}$. On the other hand, the relations required ultimately by the local gauge invariance $n_I + n_L = 1$ and $n_{L} = n_{o}$ are nearly satisfied at $r = 1$ only when $n_d^{(1)}$ is small, i.e., the theory then converges quickly. It is therefore important to keep in mind that [3,6] $n_d^{(1)} \approx \frac{1}{2}$ at $|x|$ small for $tpd \gg A_{pd}$ and that finite $tpd$ decreases it [8] further. The overall rule of thumb is that $n_d^{(1)} < \frac{1}{2}$ as long as the HF chemical potential $\mu^{(1)}$ falls below the VH singularity in the lowest L-band, i.e., as long as $x < x_{vH}$ where [8] $x_{vH} \propto -tpd$ is the positive doping required to reach the VH singularity. As easily seen, small $n_d^{(1)}$ corresponds to a weak effective interaction $\bar{U} < t_{pd}$.

The Cu–O (anti)commutation rules are also irrelevant for two further $r = 2, 3$ expressions. $r = 2$ leads to the coherent Brinkman–Rice-like band narrowing $t_{pd}^2 \rightarrow t_{pd}^2(1 + n_d/2)(1 - n_d)$ and the variation of $A_{pd}$ through $n_d \rightarrow \bar{q}_{vH}$. However, unlike in the mean-field [8–10] slave particle approximations, this is accompanied by the incoherent, local, dynamic fluctuations identified as the $d_{10} \leftrightarrow d_{8}$ charge-transfer disorder. Importantly, the disorder falls far from the Fermi level, although there are indications [10–12] that in higher perturbation orders it spreads all over the spectrum.

The interaction $\bar{U}$ appears explicitly for $r = 4$. It introduces the particle–particle and particle–hole correlations in the single particle $tpd$ and $dpd$ propagations. $\bar{U} > 0$ favors the coherent particle–hole correlations which appear here as pseudogaps. The slave fermion theory predicts however that the effect of $\bar{U}$ is the same in the singlet and the triplet channels, which is the consequence of the omission of the Cu–O anticommutation rules.

3. Coherent e–h correlations and stripes

Let us start with the SDW correlations for $x = x_{vH} > 0$. The VH overlap/FS nesting behavior of the elementary intraband particle–hole bubble is not universal. It is however well known that $R_{X_{SDW}}(q, \omega)$ becomes large for $\omega$ small and close to $\pi/a$ [1,1]. Taking formally $tpd = 0$, the log square singularity in $\omega$ occurs [5,3] at $x = 0$ due to the VH overlap and to the perfect 2D FS nesting at $q_{SDW} = \pi/a$ [1,1]. Analytical [14] and numerical [15] calculations show that imperfect nesting associated with finite $x$ at $tpd = 0$ produces spikes at incommensurate $q_{SDW}$ along the zone main axes. With finite $tpd$ the spikes were also obtained numerically [16] for $q_{SDW}$ along its diagonals. While it seems well established [17] that the spikes at $q_{SDW}$ are dominated by the pairing of holes and electrons close to the antinodal $\pi/a$ [1,0] and $\pi/a$ [0,1] VH points, the pairing which gives rise to the spikes at $q_{SDW}$ is not yet determined unambiguously.

The single well-defined collinear $\pm q_{SDW}$ leg or the nearly circular $|q_{SDW}|$ is observed clearly by the magnetic neutron scattering [18–20]. As a rule, $q_{SDW}$ appears for small energy transfers while $q_{SDW}$ occurs at high frequencies, e.g., in metallic YBCO [19]. The observation of the strong leading harmonics is consistent with metallic coherency in the propagation of $tpd$-hybridized particles. There is however also good NMR evidence [21] that non-magnetic disorder is present in LSCO. It may well correspond, in part, to the local $d_{10} \leftrightarrow d_{8}$ charge-transfer disorder, which is dynamic in the present theory but becomes frozen [21,22] by the strong coupling [23] to the heavy lattice.

The Emery model also encompasses [23] the CuO$_2$ and $O_{2/3}$ charge transfers and various bond fluctuations within the unit cell. In the $\bar{q} \rightarrow 0$ limit the $D_4$ symmetry classifies [24–26] those correlations in $A_{9g}$, $B_{1g}$ and $B_{2g}$ irreducible representations, the bond fluctuations being involved directly [26] into the Raman responses. The elementary bubbles associated with those correlations differ through coherence factors in their numerators while their respective poles and integration ranges are the same [26]. The $\bar{q} = 0$ $B_{1g2g}$ modes are dominated [26], respectively, by the
conclusions from the main axes or diagonals of the CuO$_2$ zone. They have their own small q structures [15,16] (e.g., the elementary O$_y$/O$_x$ bubble is logarithmically singular [23] at \( x = x_{sdw} \)). In addition, while the \( \bar{q} \approx 0 \) B$_x$ and B$_y$ intercell modes are decoupled from the \( q \approx 0 \) transfers of the total CuO$_2$ charge among the distant unit cells [15,23,26], the coherent \( \bar{q} \approx 0 \) CuO$_2$/charge transfer is accompanied [15,26] by the \( \approx 0 \) intercell charge transfer. Only the latter is subject to the long-range Coulomb screening/frustration [15,22,26,27].

The small q behavior of the charge-transfer correlations is however of secondary interest if the SDW is taken [14] as the dominant fluctuation. Then, according to Fig. 2, two SDWs enhanced at \( \bar{q}_{sdw} \approx \pi/\alpha[1,1] \) either couple to the intracell fluctuations and then to phonons, or else directly to phonons. In the case of linear coupling of Fig. 2a the corresponding dominant \( q_0 \) is small and satisfies the physically important relation

\[
\frac{q_0}{\pi} + 2\pi/\alpha[1,1] = 2\bar{q}_{sdw}.
\]

Alternatively, as in Fig. 2b, two such SDWs can also couple quadratically [23] to tilts of the CuO$_2$ octahedra at \( \bar{q}_{tilt} = \bar{q}_{sdw} \). When two SDWs enhanced at \( \bar{q}_{sdw} \) close to \( \pi/\alpha[1,1] \) are associated with the \( \pi/\alpha[1,0], \pi/\alpha[0,1] \) pairing they drive [26], via the B$_x$ O$_y$/O$_x$ charge transfer, the LTT/\( \langle ex-x_y \rangle \) deformations at \( \pm \bar{q}_{tilt} \) or \( \pm \bar{q}_{sdw} \). Analogously, if two SDWs enhanced at \( \bar{q}_{sdw} \) close to \( \pi/\alpha[1,1] \) are associated with the \( \pi/\alpha[1,1], \pi/\alpha[1,1] \) pairing they drive [26] the B$_y$ O$_x$/O$_y$ bond fluctuations and the LTO/\( \langle e_y + e_x \rangle \) modes at \( \pm \bar{q}_{tilt} \) or \( \pm \bar{q}_{sdw} \).

The \( \bar{q}_{tilt} \approx \pi/\alpha[1,1] \) tilts and the \( \bar{q}_0 \) modes are in addition entangled [28] by the ionic forces, namely the \( \pi/\alpha[1,1] \) LTT and LTO tilts are accompanied, respectively, by the homogeneous \( e_x \) and \( e_y \) shear of the CuO$_2$ planes. Those entangled single-leg deformations thus lift, through the electron–phonon couplings [23], the degeneracy of two O$_x$/O$_y$ sites [23] or of four \( t_{2g} \) bonds within the CuO$_2$ unit cell by dimerizing them two by two.

The stability of the striped structures can be investigated using the related [14,23] Landau functionals. E.g., the entangled collinear modes are related in this way to the collinear nematic static stripes [27,29] usually characterized by \( q_{coll} \). It appears thus quite clearly that the coherent O$_x$/O$_y$ charge transfer, coupled to the lattice, is an essential ingredient of the collinear stripes [27] in the metallic phase. This agrees with observations [18,19,24,25,30,31]. The collinear SDW and O$_y$/O$_x$ charge-transfer correlations get enhanced in metallic lanthanum cuprates for dopings \( x \approx x_{sdw} \). The spikes [17] at \( \bar{q}_{sdw} \) and \( \bar{q}_{tilt} \) then explain the “nematic” version of Eq. (2) observed [18,24] in the metallic phase. The corresponding LTO/LTT lattice instability is predicted [23] and observed [32,33] to be of the first order in LBCO for \( x \approx x_{sdw} \). Those effects are attributed here to the \( \bar{q}_{tilt} \) overlap/FS nesting, while the commensurability \( q_{coll} \) is expected to play only the secondary role.

In contrast to lanthanum cuprates the Fermi level \( \mu \) in the optimally doped YBCO and BSCO, as measured by ARPES, falls [8] well below the \( \bar{q}_{tilt} \) point, i.e., \( x < x_{sdw} \). The collinear SDW-O$_x$/O$_y$ stripes enhanced by the \( \bar{q}_{tilt} \) singularities are therefore not expected to occur in metallic YBCO and BSCO. Indeed, at larger \( x \), the collinear stripe structure is replaced [25] by the fourfold commensurate stripes in “checkerboard” configuration [25,34], which restores the D$_x$ symmetry.

The salient new feature of the present low-order large \( U \) analysis is thus that the coherent, weak, incommensurate collinear [17] SDW and O$_x$/O$_y$ correlations appear to get enhanced with respect to the \( \bar{q}_{tilt} \) and \( \bar{q}_{sdw} \) charge disorder if the \( \bar{q}_{tilt} \) singularities are reached [35] by doping \( x_{sdw} \). This explains the long standing puzzle [32] why the enhanced magnetic/charge coherence occurs twice in LBCO as a function of doping, once as the long- or short-range [4,36] AF order at \( x = 0 \) and then again as the incommensurate SDW at single \( \pm \bar{q}_{sdw} \) for finite positive \( x_{sdw} \approx 0.1 \), accompanied by the static O$_y$/O$_x$ charge transfer coupled to the staggered LTT tilting of the CuO$_2$ octahedra.

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References